Fracral Reconstruction of Dilaton Field

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Abstract

Numerous papers have been presented [1,2,3,4,5] to implement the dynamics of scalar field describing nature of the dark energy by establishing a connection between the pilgrim/new agegraphic/Ricci/ghost/holographic energy density and a scalar field definition. These works showed that the analytical form of potential in terms of the scalar field cannot be obtained due to the complexity of the involved equations. On the other hand, writing a meaningful quantum gravity theory is one of the tough puzzles in modern theoretical physics [6,7]. In the quantum gravity theories, the universe is described as a dimensional flow and one can discuss whether and how these attractive features are connected with the ultraviolet-divergence problem [8]. That's why, such important points motivated us to reconstruct the potential and dynamics of the dilaton scalar field model [9] according to the evolutionary behavior of the extended holographic energy description [10] in fractal geometry.

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The Cauchy Problem for Complex Intuitionistic Fuzzy Differential Equations

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Abstract

In this paper, we discuss the existence of a solution to the Cauchy problem for complex intuitionistic fuzzy differential equations. We first propose definitions of complex intuitionistic fuzzy sets and discuss entailed results which parallel those of complex fuzzy sets.

Keywords : complex intuitionistic fuzzy sets, complex intuitionistic fuzzy differential equations.

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